

ΜΑΘΗΜΑ: Φυσική προσανατολισμού

ΘΕΜΑ Α

A1. γ

A2. δ

A3. γ

A4. β

A4. α. Λάθος

β. Σωστό

γ. Λάθος

δ. Σωστό

δ. Σωστό

ΘΕΜΑ Β

B1. 1^η ΠΕΡΙΠΤΩΣΗ:

$$\Theta.\Sigma. \Sigma F = 0 \Rightarrow F_{E\lambda} = w \Rightarrow kA_1 = mg \Rightarrow A_1 = \frac{mg}{k}$$

2^η ΠΕΡΙΠΤΩΣΗ:

$$\Theta.\Sigma. \Sigma F = 0 \Rightarrow F_{E\lambda}' + F = w \Rightarrow F_{E\lambda}' = 0$$

Άρα η Θ.Φ.Μ. είναι η Θ.Ι.

Ενώ η παλιά Θ.Ι. είναι η Α.Θ. αφού $u = 0$

Άρα $A_1 = A_2$

Σωστή απάντηση είναι η (i)

$$\text{B2. } P_{\text{atm}} + 0 + \rho g H = P_{\text{atm}} + \frac{1}{2} \rho u_1^2 + \rho g \frac{5H}{6} \Rightarrow$$

$$\Rightarrow \frac{1}{2} \rho u_1^2 = \rho g \frac{H}{6} \Rightarrow u_1^2 = \frac{gH}{3} \Rightarrow u_1 = \sqrt{\frac{gH}{3}}$$

$$\Pi_1 = A u_1 = A \sqrt{\frac{gH}{3}}$$

$$P_{\text{atm}} + 0 + \rho g H = P_{\text{atm}} + \frac{1}{2} \rho u_2^2 + \rho g \frac{H}{3} \Rightarrow$$

$$\Rightarrow \frac{1}{2} \rho u_2^2 = \rho g \frac{2H}{3} \Rightarrow u_2 = 2 \sqrt{\frac{gH}{3}}$$

$$u_2 = 2u_1 \Rightarrow \Pi_2 = 2\Pi_1$$

$$\Pi_1 = \frac{V}{\Delta t_1} \quad \Pi = \Pi_1 + \Pi_2 = 3\Pi_1$$

$$\Pi = \frac{V}{\Delta t_2} \Rightarrow 3\Pi_1 = \frac{V}{\Delta t_2}$$

$$3 \frac{V}{\Delta t_1} = \frac{V}{\Delta t_2} \Rightarrow \frac{\Delta t_2}{\Delta t_1} = \frac{1}{3}$$

Σωστή απάντηση είναι η (ii)

$$\text{B3. } P_1 = m_1 u_1$$

$$P_1' = \frac{P_1}{5} \Rightarrow m_1 u_1' = \frac{m_1 u_1}{5} \Rightarrow u_1' = \frac{u_1}{5}$$

$$u_1' = \frac{m_1 - m_2}{m_1 + m_2} u_1 \Rightarrow \frac{u_1}{5} = \frac{m_1 - m_2}{m_1 + m_2} u_1 \Rightarrow 5m_1 - 5m_2 = m_1 + m_2 \Rightarrow$$

$$\Rightarrow 4m_1 = 6m_2 \Rightarrow m_1 = \frac{3}{2} m_2$$

$$u_2' = \frac{2m_1}{m_1 + m_2} u_1 \Rightarrow u_2' = \frac{2 \cdot \frac{3}{2} m_2}{\frac{3}{2} m_2 + m_2} u_1 = \frac{3m_2}{\frac{5}{2} m_2} u_1 = \frac{6}{5} u_1$$

$$K_1 \rightarrow K_2' \Rightarrow \frac{1/2 m_2 u_2'^2}{100 \rightarrow \Pi\%} = \frac{1/2 m_1 u_1^2}{100\%} \Rightarrow \frac{m_2 \left(\frac{6}{5} u_1\right)^2}{\frac{3}{2} m_2 u_1^2} \cdot 100\% \Rightarrow$$

$$\Rightarrow \Pi\% = \frac{36}{25} \cdot 100\% = \frac{72}{25} \cdot 100\% = \frac{72 \cdot 4}{25} \% = 96\%$$

Σωστή απάντηση είναι η (iii)

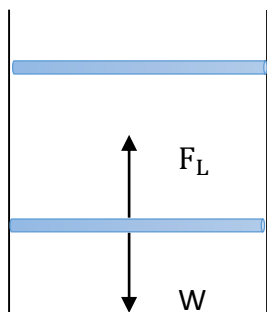
Θέμα Γ

Γ1. Ν. Ohm: $I = \frac{E}{R_{ολ}} = \frac{9}{3} = 3A$

Ισορροπία : $\Sigma F = 0 \Rightarrow W - F_L = 0 \Rightarrow W = F_L \Rightarrow mg = BI\ell \Rightarrow B = 1T$

με κατεύθυνση, σύμφωνα με τον κανόνα των τριών δακτύλων, από τον αναγνώστη προς τη σελίδα.

Γ2.



$$\Sigma F = m \cdot \alpha \Rightarrow w - F_L = m \cdot \alpha \Rightarrow \alpha = \frac{w - F_L}{m}$$

Το είδος της κίνησης είναι: Μη ομαλά επιταχυνόμενη με επιτάχυνση που διαρκώς μειώνεται, λόγω αύξησης της F_L .

$$\Sigma F = 0 \Rightarrow F_L = W \Rightarrow$$

$$\frac{B^2 \cdot U_{ορ} \cdot \ell^2}{R_{ολ}} = mg \Rightarrow U_{ορ} = 3 \cdot 4 = 12m/s$$

$$P_K = \frac{V_K^2}{R_K} \Rightarrow R_K = \frac{V_K^2}{P_K} = \frac{36}{6} \Omega = 6\Omega$$

$$R_{ολ} = \frac{R_1 \cdot R_\Sigma}{R_1 + R_\Sigma} + R_{K\Lambda} = \left(\frac{18}{9} + 2\right) \Omega = 4\Omega$$

Γ3. $\frac{dp}{dt} = \Sigma F = W - F_L = mg - BI\ell$

$$U = \frac{U_0}{2} = 6m/s$$

$$F_L = BI\ell = \frac{B^2 \cdot U \cdot \ell^2}{R_{ολ}} = \frac{1 \cdot 6 \cdot 1}{4} N = 1,5N$$

Γ4. Όταν $U_{op} = 12m/s$

Για να λειτουργεί κανονικά πρέπει $I_K = I_{επ}$

$$P_K = V_K \cdot I_K \Rightarrow I_K = \frac{P_K}{V_K} = 1A$$

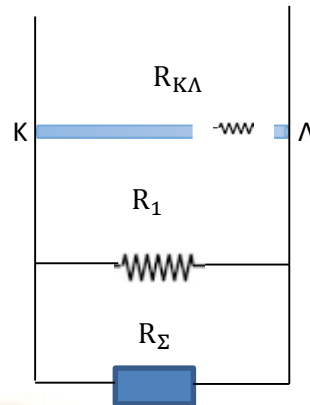
$$E_{επ} = BU\ell = 1 \cdot 12 \cdot 1 = 12V$$

$$I_{επ} = \frac{E_{επ}}{R_{ολ}} = \frac{12}{4} A = 3A$$

$$V_{K\Lambda} = E - Ir = 12 - 3 \cdot 2 = 6V$$

Η σύνδεση είναι παράλληλη άρα $V_{K\Lambda} = V_{\Sigma} = V_1$

$$I = \frac{V_{K\Lambda}}{R_{\Sigma}} = \frac{6}{6} = 1A, \text{ άρα θα λειτουργεί κανονικά.}$$



Θέμα Δ

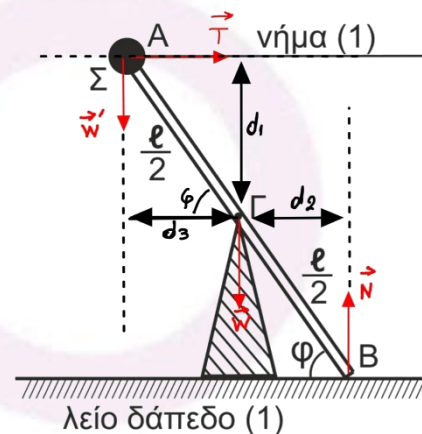
Δ1. $\Sigma\tau = 0 \Rightarrow -T \cdot d_1 + N \cdot d_2 + W_1 \cdot d_3 = 0 \Rightarrow$

$$\Rightarrow -T \cdot \frac{\ell}{2} \cdot \eta\mu\varphi + N \cdot \frac{L}{2} \cdot \sigma\upsilon\upsilon\varphi + mg \cdot \frac{L}{2} \cdot \sigma\upsilon\upsilon\varphi = 0$$

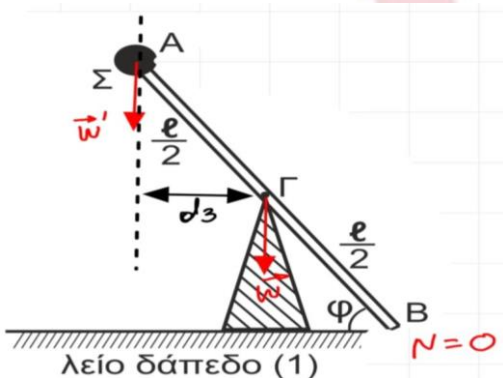
$$\Rightarrow -10,5 \cdot \frac{2}{2} \cdot 0,8 + N \cdot \frac{2}{2} \cdot 0,6 + 10 \cdot \frac{2}{2} \cdot 0,6 = 0$$

$$\Rightarrow -8,4 + 0,6N + 6 = 0 \Rightarrow 0,6N = 8,4 - 6 \Rightarrow$$

$$N = 4N$$



Δ2.



$$\Sigma\tau = I \cdot \alpha_{\gamma\omega\nu} \quad (1)$$

$$I_{O\Lambda} = I_p + I_m = \frac{1}{12} M_p \cdot R^2 + m \left(\frac{\ell}{2}\right)^2 = \frac{1}{12} \cdot 3 \cdot 4 + 1 \cdot 1$$

$$= 2kg \cdot m^2$$

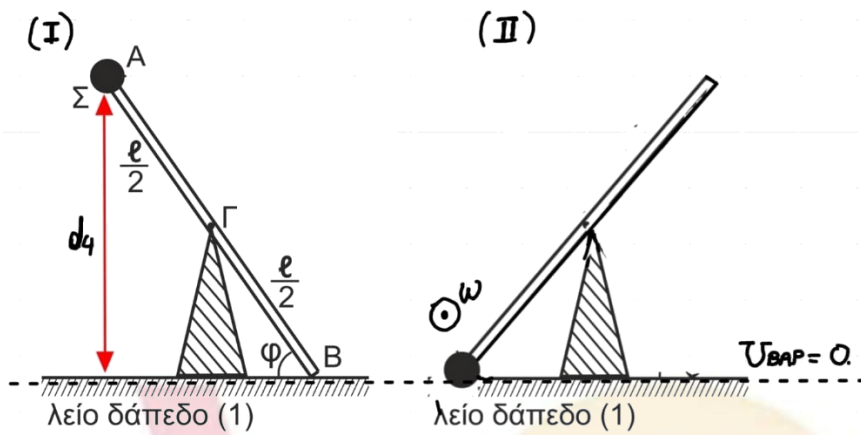
$$(1) \Rightarrow W_1 \cdot d_3 = I_{O\Lambda} \cdot \alpha_{\gamma\omega\nu} \Rightarrow$$

$$\Rightarrow m_1 g \cdot \frac{\ell}{2} \sigma\upsilon\upsilon\varphi = I_{O\Lambda} \cdot \alpha_{\gamma\omega\nu}$$

$$\Rightarrow 10 \cdot 0,6 = 2 \cdot \alpha_{\gamma\omega\nu} \Rightarrow \alpha_{\gamma\omega\nu} = 3m/s^2$$

$$\left. \frac{dL}{dt} \right|_M = I_M \cdot \alpha_{\gamma\omega\nu} = 1 \cdot 3 = 3kg \cdot m^2/s^2$$

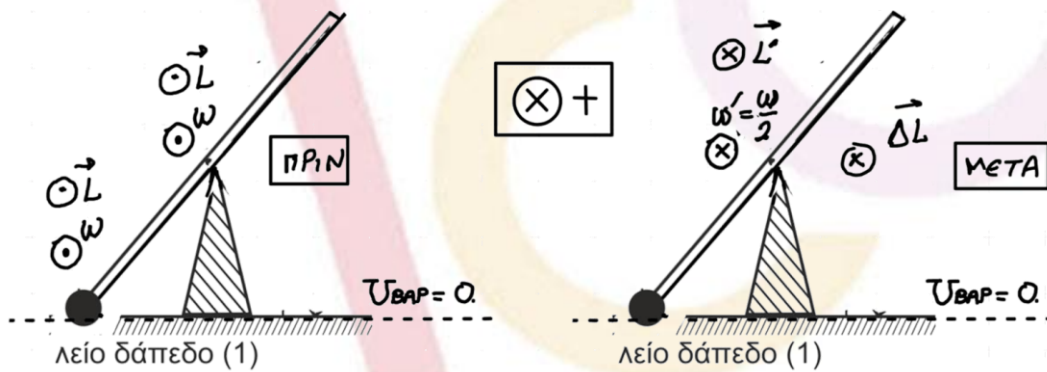
Δ3.



ΘΜΚΕ για το σύστημα:

$$K_{\text{τελ}} - K_{\text{αρχ}} = W_{\text{ΣF}} \Rightarrow \frac{1}{2} \cdot I_{\text{ΣΥΣ}} \cdot \omega^2 = W_{W_1} + W_{W_{\rho\alpha\beta\delta}} \Rightarrow$$

$$\Rightarrow \frac{1}{2} \cdot 2 \cdot \omega^2 = mgd_4 - 0 \Rightarrow \omega^2 = 1 \cdot 10 \cdot 1,6 \Rightarrow \omega = 4 \text{ rad/s}$$



$$\Delta L_{\text{ΣΥΣ}} = L_{\text{ΤΕΛ}} - L_{\text{ΑΡΧ}} = I_{\text{ΣΥΣ}} \cdot \omega' - (-I_{\text{ΣΥΣ}} \cdot \omega) = I_{\text{ΣΥΣ}} \cdot \frac{\omega}{2} + I_{\text{ΣΥΣ}} \cdot \omega = I_{\text{ΣΥΣ}} \left(\omega + \frac{\omega}{2} \right) =$$

$$I_{\text{ΣΥΣ}} \cdot \frac{3\omega}{2} = 2 \cdot \frac{3 \cdot 4}{2} = 12 \text{ kg} \cdot \text{m}^2/\text{s}$$

Δ4. $\Sigma \vec{F}_x = m \cdot \vec{a} \Rightarrow \boxed{F + T_{\sigma\tau} = M \cdot \alpha_{CM}}$ (1)

$\Sigma \tau_{(O)} = I_{(O)} \cdot \alpha_{\gamma\omega\nu} \Rightarrow \boxed{F \cdot r - T_{\sigma\tau} \cdot R = \frac{1}{2} M_T \cdot R^2 \cdot \alpha_{\gamma\omega\nu}}$ (2)

(1) $\Rightarrow F \cdot R + \cancel{T_{\sigma\tau} \cdot R} = M_T \cdot R \cdot \alpha_{CM}$ λόγω κ.χ.ο.
 $\alpha_{CM} = \alpha_{\gamma\omega\nu} \cdot R$
 \Rightarrow

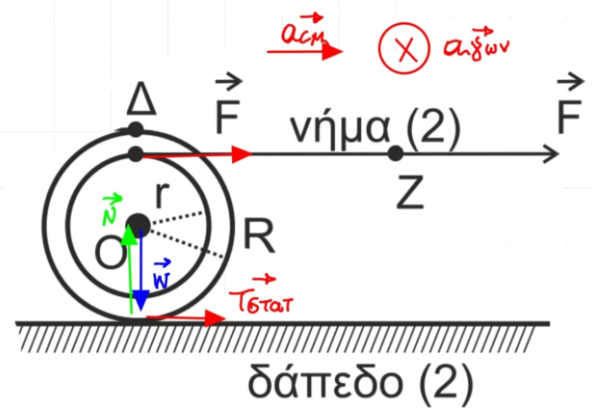
(2) $\Rightarrow F \cdot r - \cancel{T_{\sigma\tau} \cdot R} = \frac{1}{2} M_T \cdot R^2 \cdot \alpha_{\gamma\omega\nu}$

$\Rightarrow F(R+r) = M_T \cdot R^2 \cdot \alpha_{\gamma\omega\nu} + \frac{1}{2} M_T \cdot R^2 \cdot \alpha_{\gamma\omega\nu}$

$\Rightarrow 12(0,4+0,3) = \frac{3}{2} M_T \cdot R^2 \cdot \alpha_{\gamma\omega\nu} \Rightarrow$

$\Rightarrow 12 \cdot 0,7 = \frac{3}{2} \cdot 7 \cdot \frac{16}{100} \cdot \alpha_{\gamma\omega\nu} \Rightarrow 1,2 = \frac{48}{200} \cdot \alpha_{\gamma\omega\nu} \Rightarrow \alpha_{\gamma\omega\nu} = 5 \frac{\text{rad}}{\text{s}^2}$

$\alpha_{CM} = \alpha_{\gamma\omega\nu} \cdot R = 5 \cdot 0,4 = 2 \frac{\text{m}}{\text{s}^2}$



Δ5. $t_1 = 2\text{s}$ $S = \frac{1}{2} \alpha_{CM} \cdot t^2 = \frac{1}{2} \cdot 2 \cdot 2^2 = 4 \text{ m}$

$W_F = F \cdot S + \tau_F \cdot \theta$

$= F \cdot S + F \cdot r \cdot \theta =$

$= 12 \cdot 4 + 12 \cdot 0,3 \cdot 10 = 48 \cdot 36 = 84 \text{ J}$

$S = \theta \cdot R$

$4 = \theta \cdot 0,4$

$\theta = 10 \text{ rad}$